

Theorie der Programmiersprachen, Übung 2 – Johannes Rössel, Klaus Grohnwaldt, Johanna Frank

$$\frac{\frac{[ass_1]}{\langle z := 0, s \rangle \rightarrow s [x \rightarrow 17, y \rightarrow 5, z \rightarrow 0]} \quad (1)}{\langle z := 0; \text{ while } y \leq x \text{ do } z := z + 1; x := x - y \text{ end}, s \rangle \rightarrow s [x \rightarrow 2, y \rightarrow 5, z \rightarrow 3]} [comp]$$

$$\frac{\frac{\frac{[ass_1]}{\langle z := z + 1, s [x \rightarrow 17, y \rightarrow 5, z \rightarrow 0] \rangle \rightarrow s [x \rightarrow 17, y \rightarrow 5, z \rightarrow 1]} \quad \frac{[ass_1]}{\langle x := x - y, s [x \rightarrow 17, y \rightarrow 5, z \rightarrow 1] \rangle \rightarrow s [x \rightarrow 12, y \rightarrow 5, z \rightarrow 1]} [comp]}{\langle z := z + 1; x := x - y, s [x \rightarrow 17, y \rightarrow 5, z \rightarrow 0] \rangle \rightarrow s [x \rightarrow 12, y \rightarrow 5, z \rightarrow 1]} \quad (2)}{\langle \text{ while } y \leq x \text{ do } z := z + 1; x := x - y \text{ end}, s [x \rightarrow 17, y \rightarrow 5, z \rightarrow 0] \rangle \rightarrow s [x \rightarrow 2, y \rightarrow 5, z \rightarrow 3]} [while_1]$$

$$\frac{\frac{\frac{[ass_1]}{\langle z := z + 1, s [x \rightarrow 12, y \rightarrow 5, z \rightarrow 1] \rangle \rightarrow s [x \rightarrow 12, y \rightarrow 5, z \rightarrow 2]} \quad \frac{[ass_1]}{\langle x := x - y, s [x \rightarrow 12, y \rightarrow 5, z \rightarrow 2] \rangle \rightarrow s [x \rightarrow 7, y \rightarrow 5, z \rightarrow 2]} [comp]}{\langle z := z + 1; x := x - y, s [x \rightarrow 12, y \rightarrow 5, z \rightarrow 1] \rangle \rightarrow s [x \rightarrow 7, y \rightarrow 5, z \rightarrow 2]} \quad (3)}{\langle \text{ while } y \leq x \text{ do } z := z + 1; x := x - y \text{ end}, s [x \rightarrow 12, y \rightarrow 5, z \rightarrow 1] \rangle \rightarrow s [x \rightarrow 2, y \rightarrow 5, z \rightarrow 3]} [while_1]$$

$$\frac{\frac{\frac{[ass_1]}{\langle z := z + 1, s [x \rightarrow 7, y \rightarrow 5, z \rightarrow 2] \rangle \rightarrow s [x \rightarrow 7, y \rightarrow 5, z \rightarrow 3]} \quad \frac{[ass_1]}{\langle x := x - y, s [x \rightarrow 7, y \rightarrow 5, z \rightarrow 3] \rangle \rightarrow s [x \rightarrow 2, y \rightarrow 5, z \rightarrow 3]} [comp]}{\langle z := z + 1; x := x - y, s [x \rightarrow 7, y \rightarrow 5, z \rightarrow 2] \rangle \rightarrow s [x \rightarrow 2, y \rightarrow 5, z \rightarrow 3]} \quad (4)}{\langle \text{ while } y \leq x \text{ do } z := z + 1; x := x - y \text{ end}, s [x \rightarrow 12, y \rightarrow 5, z \rightarrow 2] \rangle \rightarrow s [x \rightarrow 2, y \rightarrow 5, z \rightarrow 3]} [while_1]$$

$$\frac{[while_2]}{\langle \text{ while } y \leq x \text{ do } z := z + 1; x := x - y \text{ end}, s [x \rightarrow 2, y \rightarrow 5, z \rightarrow 3] \rangle \rightarrow s [x \rightarrow 2, y \rightarrow 5, z \rightarrow 3]} \quad (4)$$